

**Mathematics, Physics
and Finance for the
Legal Profession**

Mathematics, Physics and Finance for the Legal Profession

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*Dedicated to:
Rene Descartes, Sir Isaac Newton, Albert Einstein, and Cupcake*

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Preface

The subject matter can be deceiving, not with respect to content, which is quite clear from the title, but rather with respect to difficulty and tediousness. Moreover, the book is designed to take an important trio of crucial topics and spoon feed them as comfortably as possible to the people who need them the most but like them the least—law students. Many jokingly state that they became law students because they couldn't handle numbers in college. A rude awakening, however, confronts them in practice, where numbers become the primary focus of what they do.

As the first pedagogical book combining the subjects of Mathematics, Physics, Finance and Law, this treatise is built on the notion that lawyers are ill prepared to face the world dominated by numbers and the multitudes who know how to distort and misrepresent them. Thieves such as Bernie Maddof, who managed to deceive the entire legal staff of the Securities and Exchange Commission for decades, were not merely flukes.

Using a similarly named course (“*Mathematics, Physics and Numbers for Lawyers*”), I experimented with the cases and subjects in order to best determine how to capture and maintain the students' interest, while at the same time building confidence in skills that are otherwise foreign to law school curricula. Nearly every chapter of the book contains some material that lawyers must possess; some of the information is indispensable. Like it or not, we all live in a scientific world, a digital world—one that is ruled by numbers, equations, formulas and statistics.

The chapter headings and subtitles present some of the most complex and baffling subjects that confront today's scientists. Students are urged not to be afraid. The book provides the softest approaches possible.

Cases have been edited, some severely due to size constraints. Where it was to possible to do so seamlessly, I have omitted annoying ellipses, asterisks and “*citations omitted*” messages.

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